Solubility

Our start in adventures in Aqueous Equilibria

SAME AS EQUIL.

Sea Shells are essentially Calcium Carbonate crystals held together by proteins

Given this information what do you think equilibrium constant will be for this reaction?

$$CaCO_3\,(s) \longleftrightarrow Ca^{2+}(aq) + CO_3^{2-}(aq)$$

↑ Shells DONT Dissolve

A. a number much much less than 1 — Favors R

B. a number approximately equal to 1

C. a number much much larger than 1 — Favors P

We will be mostly dividing substances up

Strong Electrolyte

~ All Dissolves ex. NaCl

Weak Electrolyte

~ None Dissolves AgCl

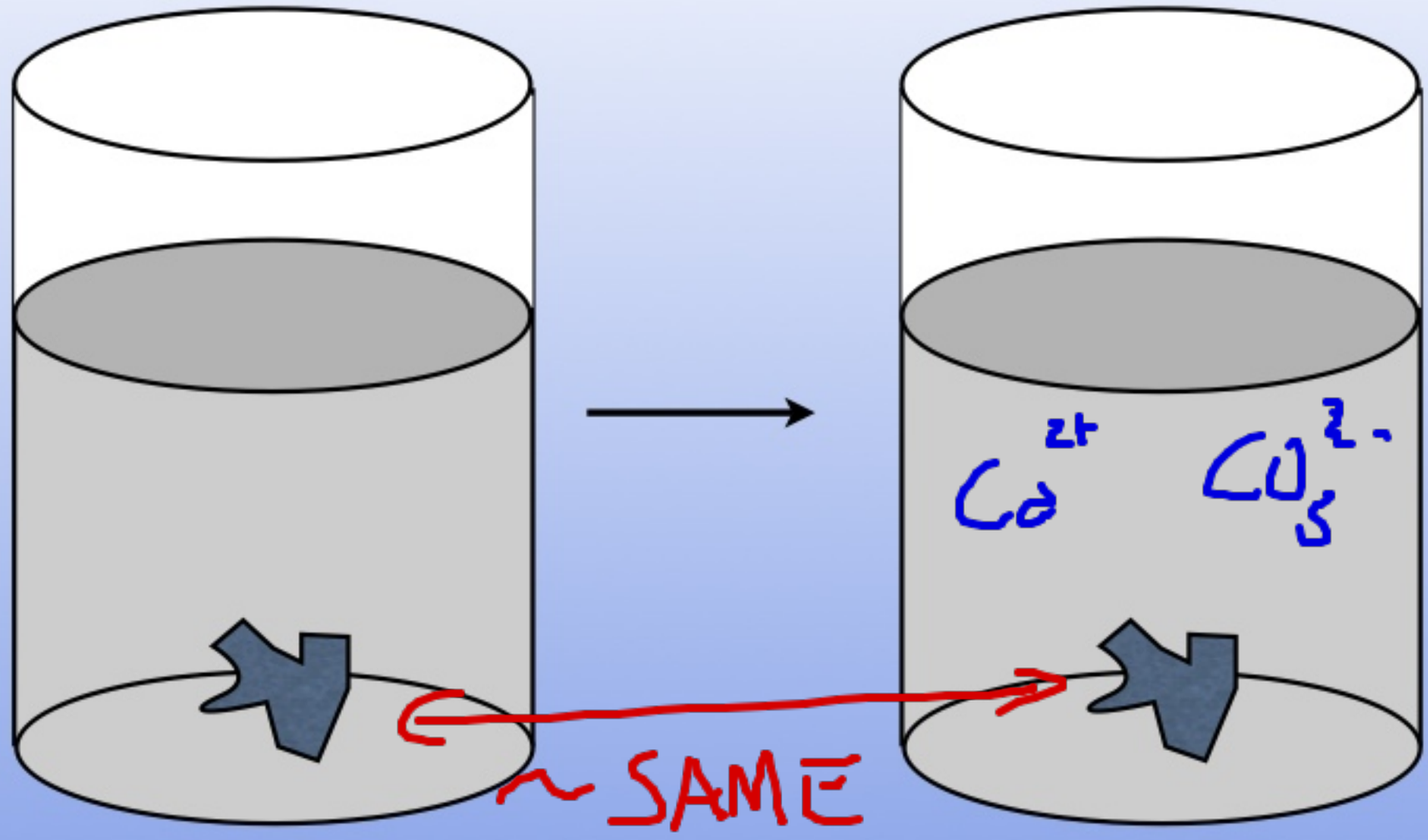
insoluble $CaCO_3$

Rock Demo

Rock Demo

$[Ca^{2+}]$ = 0

$[Ca^{2+}]$ = Very Small



How much of the rock dissolved? ~ NONE

How much is very small?
Solubility Equilibria

$$CaCO_3\,(s) \longleftrightarrow Ca^{2+}(aq) + CO_3^{2-}(aq)$$

$$K_{sp} = \frac{[Ca^{2+}][CO_3^{2-}]}{1}$$

solubility product

PRODUCT OF ION CONC.

Solubility is given in practical units

Molar Solubility

Moles of solute that will dissolve in 1 L of sovlent (water)

$$\frac{\text{Moles}}{\text{L}} \Longrightarrow \text{max concentration}$$

Solubility is given in practical units

Molar Solubility

Moles of solute that will dissolve in 1 L of sovlent (water)

MASS

Solubility

grams of solute that will dissolve in 1 L of sovlent (water)

What is the solubility of AgCl?

$$AgCl\,(s) \longleftrightarrow Ag^+(aq) + Cl^-(aq)$$

$$K_{sp} = [Ag^+][Cl^-] = 1.8 \times 10^{-10}$$

Reaction	$AgCl\,(s) \longleftrightarrow$	$Ag^+(aq)$	+ $Cl^-(aq)$
Initial		0	0
Change		+x	+x
Equilibrium		+x	+x

SAME

What is the solubility of AgCl?

$K_{sp} = [Ag^+][Cl^-] = 6 \times 10^{-9}$ 1.8×10^{-10}

Reaction	$AgCl\ (s) \longleftrightarrow$	$Ag^+(aq)$	$+ Cl^-(aq)$
Initial		0	0
Change		+x	+x
Equilibrium		+x	+x

$K_{sp} = [Ag^+][Cl^-] = (x)(x) = x^2$

$x = \sqrt{K_{sp}} = 1.3 \times 10^{-5}\ M$

What is the solubility of AgCl?

$K_{sp} = [Ag^+][Cl^-] = 1.8 \times 10^{-10}$

$AgCl(s) \longleftrightarrow Ag^+(aq) + Cl^-(aq)$

$[Ag^+] = 1.3 \times 10^{-5}\ M$

M.W. of AgCl is 143.3 g mol^{-1}

1 mole $Ag^+ \longrightarrow$ 1 mole AgCl

moles AgCl dissolved in 1 L $= 1.3 \times 10^{-5}$

g AgCl $= (143.3\ g\ mol^{-1})(1.3 \times 10^{-5}\ mol)$

$= 1.9 \times 10^{-3}\ g/L$

Which of the following compounds has the lowest molar solubility?

All form 2 ions

A. AgCl $K_{sp} = 1.8 \times 10^{-10}$

B. FeS $K_{sp} = 8 \times 10^{-19}$

C. LiF $K_{sp} = 1.8 \times 10^{-3}$

D. ZnSe $K_{sp} = 2 \times 10^{-25}$

molar solubility

$\Rightarrow x = \sqrt{K_{sp}}$

Smallest K_{sp}

lowest solubility

Which of the following compounds has the lowest molar solubility?

HARDER

A. AgCl $K_{sp} = 1.8 \times 10^{-10}$

B. $Cd_3(PO_4)_2$ $K_{sp} = 2.5 \times 10^{-30}$

5 ions

C. $Zn(OH)_2$ $K_{sp} = 3 \times 10^{-17}$

D. ZnSe $K_{sp} = 2 \times 10^{-25}$

2 ions

What is the concentration of Sr^{2+} in a saturated solution of SrF_2?

$$K_{sp} = [Sr^{2+}][F^-]^2 = 4.3 \times 10^{-9}$$

Reaction	SrF_2 (s)	$\longleftrightarrow$	Sr^{2+}(aq)	+	$2F^-$(aq)
Initial					
Change			$+x$		$+2x$
Equilibrium			$+x$		$+2x$

$$K_{sp} = (x)(2x)^2 = 4x^3$$

$$x = 10^{-3}$$

1×10^{-3}

Decent estimate of the molar solubility
count the ions
take that "root" of the K_{sp}

A. $AgCl$ $K_{sp} = 1.8 \times 10^{-10}$

2 ions $\quad x \sim \sqrt[2]{K_{sp}} \sim 10^{-5}$

B. $Cd_3(PO_4)_2$ $K_{sp} = 2.5 \times 10^{-30}$

5 ions $\quad x \sim \sqrt[5]{K_{sp}} \sim 10^{-6}$

C. $Zn(OH)_2$ $K_{sp} = 3 \times 10^{-17}$

3 ions $\quad x \sim \sqrt[3]{K_{sp}} \sim 10^{-6}$

D. $ZnSe$ $K_{sp} = 2 \times 10^{-25}$

2 ions $\quad x = \sqrt{K_{sp}} \sim 10^{-12}$

Given that K_{sp} for AgCl is 1.8×10^{-10},
and the NaCl is strong electrolyte

What do you predict for solubility of AgCl in a 1 M NaCl solution?

$K_{sp} = [Ag^+][Cl^-]$

A. more soluble than in pure water

B. same solubility as pure water

C. lower solubility than pure water

Add Products (Cl^-)

Shift to R

AgCl(s)

Given that K_{sp} for AgCl is 1.8×10^{-10},
and the NaCl is strong electrolyte

What is the concentration of Ag^+ in a 1 M NaCl solution
that contains solid AgCl?

$K_{sp} = [Ag^+][Cl^-]$ $[Ag^+] = K_{sp} / [Cl^-]$

A. 1.8×10^{-10} M

B. 1.8×10^{-6} M

C. 1.3×10^{-5} M

D. 1 M

$[Ag^+] = \frac{1.8 \cdot 10^{-10}}{1}$

What about Cl^- from AgCl?

What is the solubility of AgCl?

$K_{sp} = [Ag^+][Cl^-] = 6 \times 10^{-9}$ $1.8 \cdot 10^{-10}$

Reaction	$AgCl(s) \longleftrightarrow$	$Ag^+(aq)$	$+ Cl^-(aq)$
Initial		0	
Change		+x	+x
Equilibrium		+x	|+x

Very small

$K_{sp} = [Ag^+][Cl^-] = (x)(1+x) = 1.8 \times 10^{-10}$

$x \ll 1 \quad \therefore \quad 1+x \approx 1$ IGNORE Cl^- From AgCl

$(x)(1) = 1.8 \times 10^{-10}$

Silver Nitrate ($AgNO_3$) and Sodium Chloride (NaCl) are both soluble salts.

What will happen if I mix 200 mL of 1 M $AgNO_3$ solution with 100 ml of 1 M NaCl solution given that K_{sp} for AgCl is 1.8×10^{-10}

A. I'll have a solution with Ag^+, Cl^-, Na^+, and NO_3^- ions

B. some solid AgCl will form

C. both B & C

KNOW WHAT IS IN SOL'N

A few useful definitions and ideas

Precipitation

Insoluble solid that forms and drops out of solution

Spectator Ions

Ions that don't participate in the chemistry

What is soluble?

Many solubility rules
Typically K_{sp} is given for insoluble compounds

All Na^+, K^+, and NO_3^- salts are soluble

Ionic Equations

$NaCl(aq) + AgNO_3(aq)$

Spectator ions

$Na^+(aq) + Cl^-(aq) + Ag^+(aq) + NO_3^-(aq) \longrightarrow AgCl(s) + Na^+(aq) + NO_3^-(aq)$

Net ionic equation

$Ag^+(aq) + Cl^-(aq) \longleftrightarrow AgCl(s)$

IGNORE SPECTATORS

Precipitation Calculations

First take the reaction to completion
then calculate back to the equilibrium

K_{sp} is generally small.
First assume as much solid as possible forms
Then look at what "re-dissolves" into solution

If I mix a 100 mL of 1 M NaCl solution
with a 200 mL of 1 M $AgNO_3$ solution
how much solid AgCl will form (K_{sp}= 1.8 x 10^{-10})?

$$NaCl(aq) + AgNO_3(aq) \leftrightarrow AgCl(s) + NaNO_3(aq)$$

$$Ag^+(aq) + Cl^-(aq) \leftrightarrow AgCl(s)$$

Assume all the maximum amount of AgCl forms

Need to convert from concentration to moles!

$(.1\,L)(1M) = .1$ mol Cl^-

$(.2\,L)(1M) = .2$ mol Ag^+

MAX AgCl = .1 mol (run out of Cl^-)

.1 mol Ag^+ left

We assumed as much solid as possible formed
How much "redissolves" to get to equilibrium?

$K_{sp} = [Ag^+][Cl^-] = 1.8 \times 10^{-10}$

	$AgCl(s)$	$\longleftrightarrow$	$Ag^+(aq)$	+	$Cl^-(aq)$
Reaction					
Initial			0.333		0
Change			+x		+x
Equilibrium			.333+x		+x

$K_{sp} = [Ag^+][Cl^-] = (.333+x)(x) = 1.8 \times 10^{-10}$

Again x is very small $.333+x \approx .333$

$.333x = 1.8 \cdot 10^{-10}$ $x = 5.4 \cdot 10^{-10}$

$\frac{.1 \text{ mol}}{.3 \text{ L}}$ ← TOTAL VOLUME

Selective precipitation

I have a solution which contains
0.1 M $AgNO_3$ and 0.1 M $PbNO_3$.
How can I get out the silver and leave the lead behind?

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Add an anion for an insoluble salt for silver such as Cl^-
K_{sp} is 1.6×10^{-10} for AgCl

Selective precipitation

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0.1 M $AgNO_3$ and 0.1 M $PbNO_3$.
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Add an anion for an insoluble salt for silver such as Cl^-
K_{sp} is 1.6×10^{-10} for AgCl

But $PbCl_2$ is also insoluble so it will precipitate out as well
K_{sp} is 2.4×10^{-4} for $PbCl_2$

much more soluble

Selective precipitation

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0.1 M $AgNO_3$ and 0.1 M $PbNO_3$.
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K_{sp} is 2.4×10^{-4} for $PbCl_2$

The K_{sp} for AgCl is much smaller so we can selectively precipitate the AgCl

I have a solution which contains
0.1 M $AgNO_3$ and 0.1 M $PbNO_3$.
How can I get out the silver and leave the lead behind?

what is the maximum concentration of Cl^-
we can have and still have the $PbCl_2$ dissolved $K_{sp} = 2.4 \times 10^{-4}$

A. 4.9×10^{-2} M

B. 1.2×10^{-4} M

C. 2.4×10^{-4} M

D. 2.4×10^{-3} M

$$K_{sp} = [Pb^{2+}][Cl^-]^2$$

$$K_{sp} = (.1)[Cl^-]^2$$

$$[Cl^-] = \sqrt{\frac{K_{sp}}{.1}} = 4.9 \cdot 10^{-2}$$

I have a solution which contains
0.1 M $AgNO_3$ and 0.1 M $PbNO_3$.
How can I get out the silver and leave the lead behind?

If the Cl^- concentration is 4.9×10^{-2} M, what is the Ag^+ concentration?
$K_{sp} = 1.6 \times 10^{-10}$ for AgCl

A. 4.9×10^{-12} M

B. 3.2×10^{-9} M

C. 1.6×10^{-10} M

D. 2.4×10^{-3} M

$$K_{sp} = [Ag^+][Cl^-]$$

$$1.6 \cdot 10^{-8} = [Ag^+][4.9 \cdot 10^{-2}]$$

$$[Ag^+] = 3.2 \times 10^{-9} M$$

I have all of these ions in solution, do I get a precipitate?

This is just equilibrium, compare Q to K

$K_{sp} = 1.7 \times 10^{-5}$ for $PbCl_2$

I have a solution in which $[Pb^{2+}] = 10^{-2}$ M and $[Cl^-] = 10^{-2}$ M

A. some $PbCl_2$ will precipitate

B. all the $PbCl_2$ will be solution

$$Q = [Pb^{2+}][Cl^-]^2 = (10^{-2})(10^{-2})^2$$

$$Q = 10^{-6} \qquad Q < K$$ TO PROD