

# Chemical Equilibria

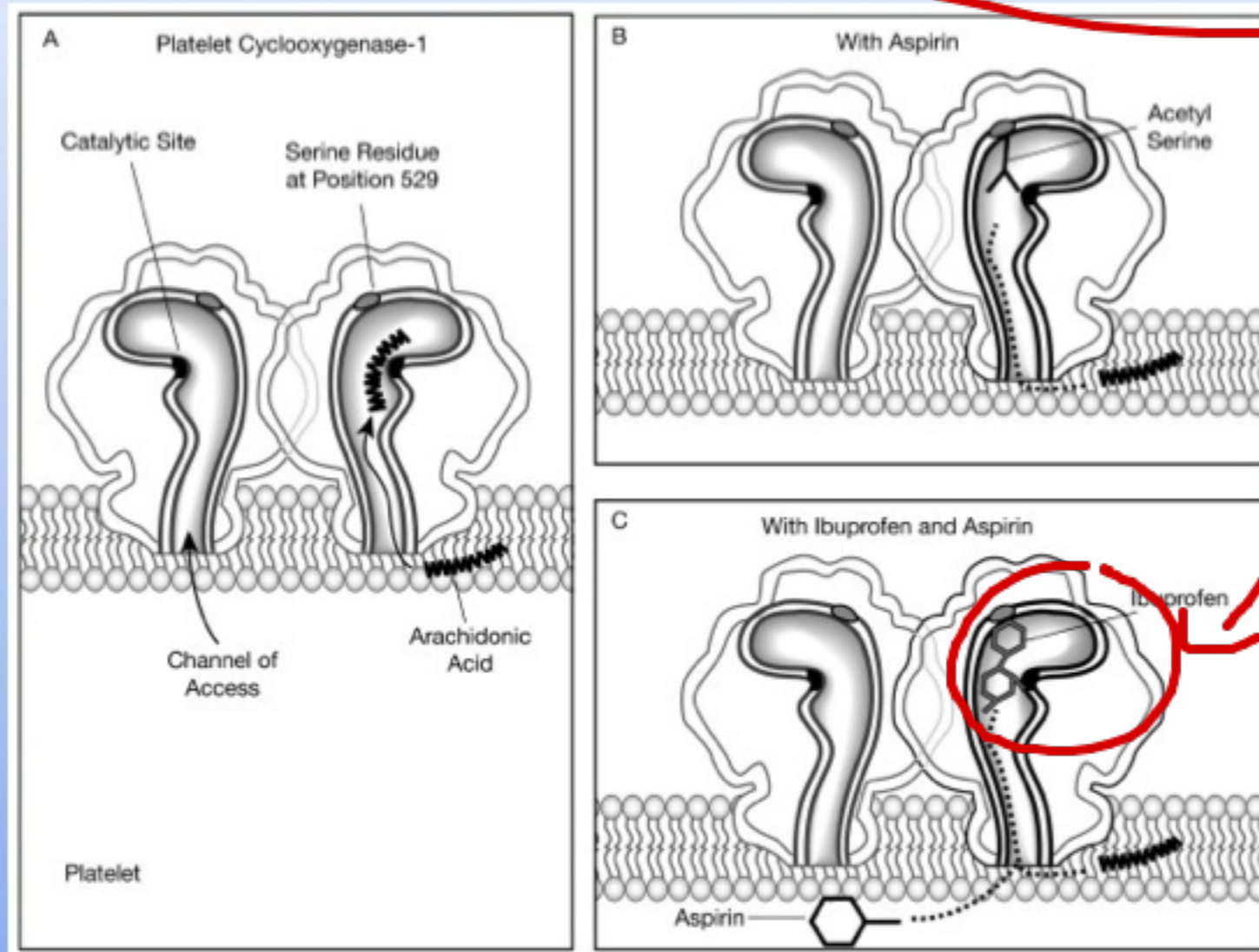
“Stress”

~~TEMP~~  
change

What happens when we try to change a chemical system at equilibrium?

Concentration  
Pressure

# What is equilibrium good for?



Blocks  
Active  
Site

Fendrick et al. *Osteopathic Medicine and Primary Care* 2008 2:2 doi:10.1186/1750-4732-2-2



For ibuprofen binding to the COX channel

$K \sim 10^8$

If we want 100x more complexed protein than free protein  
what concentration of "free" drug do we need?

A.  $10^{-8}$  M

B.  $10^{-6}$  M

C.  $10^{-4}$  M

D.  $10^{-2}$  M

$K = \frac{[\text{complex}]}{[\text{drug}][\text{protein}]} = 100$

$[\text{DRUG}] = \frac{100}{K} = 10^{-4} \text{ M}$

What is the initial concentration of Drug?



Given that  $K = 10^8$  and the initial concentration of protein is  $10^{-8}$  M

What is the maximum concentration that we can expect for the drug?

A.  $10^{-8}$  M

B.  $10^{-6}$  M

C.  $10^{-4}$  M

D.  $10^{-2}$  M

All of it!

can't be more

COMPLEX

What is the initial concentration of Drug?



Initial	$10^{-6} + x$	$10^{-8}$	0
Change	$-x$	$-x$	$+x$
Equilibrium	$10^{-6}$	$\sim 0$	$10^{-4}$

+

$\sim$  SAME

assume  
all forms  
complex

What will happen if I add more drug after my initial equilibrium?

- A. more drug will bind
- B. less drug will bind
- C. an identical amount of drug will stay bound
- D. the system will go back to equilibrium and all the concentration will return to the same values

Since the equilibrium concentration of the drug is essentially the equilibrium concentration we can easily find the new equilibrium ratio of the complex: free protein



First Equilibrium

$$[\text{Drug}] = 10^{-6} \text{ M}$$

$$10^8 K = \frac{1}{10^{-6}} \frac{[\text{complex}]}{[\text{protein}]}$$

" 100

Equilibrium after adding drug

$$[\text{Drug}] = 10^{-4} \text{ M}$$

$$K = \frac{1}{10^{-4}} \frac{\text{complex}}{\text{protein}}$$

" 10<sup>4</sup>!

## Equilibria and Perturbations (Stress)

What happens to a system at equilibrium if I change something like

The concentrations  
of one of the chemicals

The Pressure

The Temperature

$K$   
const

$K$   
changes

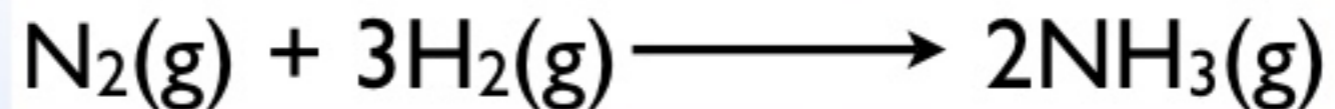


## Qualitatively Understanding "stress"

### Le Chatlier's Principle

If a chemical system at equilibrium experiences a change,

then the equilibrium shifts to partially counter-act the imposed change.



You find the system at equilibrium,  
then you decide to add more  $\text{H}_2$  to the mixture

What happens as the reaction goes to a new equilibrium?

A. the concentration of  $\text{N}_2$  decreases

B. the concentration of  $\text{NH}_3$  decreases

C. nothing when equilibrium is reached all the concentrations  
will be the same as before

$\text{H}_2 \uparrow$

TO PROD

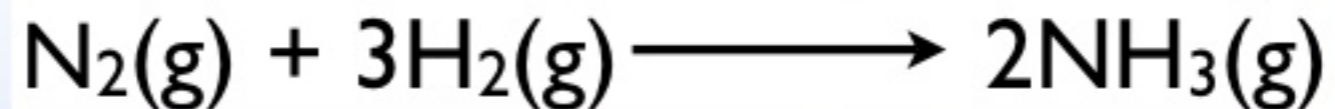
## Stressing the concentrations

Add Reactants  $\longrightarrow$  Reaction Shifts  
towards Product

Add Products  $\longrightarrow$  Reaction Shifts  
towards Reactants

Amount of pure substances doesn't matter

What if I increase the pressure?



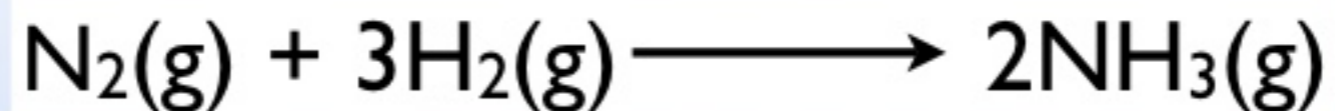
You find the system at equilibrium at 1 atm, then you decide to increase the pressure to 2 atm.

What happens as the reaction goes to a new equilibrium?

- A. moves towards the products as they have fewer molecules
- B. moves towards the reactants as they have more molecules
- C. moves towards the products as they have a lower free energy

Relieve stress. Lower P. fewer n

## Dealing with Stress from a Quantitative Perspective



Equilibrium

$$\begin{aligned}[\text{N}_2] &= 0.921 \text{ M} \\ [\text{H}_2] &= 0.763 \text{ M} \\ [\text{NH}_3] &= 0.157 \text{ M}\end{aligned}$$

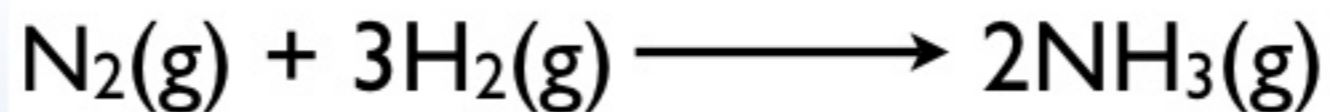
$$K_c = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3}$$

$$K_c = \frac{[0.157]^2}{[.921][.763]^3} = \underline{0.06}$$

If I increase  $[\text{N}_2]$  to 3 M the system will no longer be at equilibrium.

Which way will it shift to get back to equilibrium?

WHAT IS Q?



Not at equilibrium

not at equilibrium

$$Q = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3}$$

$$Q = \frac{[0.157]^2}{[3][.763]^3} = .0185$$

$[\text{N}_2]$

$[\text{H}_2]$

$[\text{NH}_3]$

$[\text{N}_2] = 3 \text{ M}$   
 $[\text{H}_2] = 0.763 \text{ M}$   
 $[\text{NH}_3] = 0.157 \text{ M}$

$$Q = 0.0185$$

$$K = 0.06$$

$$Q < K$$

"Too few products"

therefore reaction needs to increase products to get to equilibrium

K is constant

$$K = \frac{\text{Products}}{\text{Reactants}}$$

So if products goes up  
the reaction will shift to get  
back to the same constant ratio

This can happen if  
Product goes down slightly  
and Reactant goes up slightly

## Increasing Pressure



$$K_p = \frac{P_{\text{N}_2\text{O}_4}}{P_{\text{NO}_2}^2} = \frac{X_{\text{N}_2\text{O}_4} P}{(X_{\text{NO}_2} P)^2} = \frac{X_{\text{N}_2\text{O}_4}}{X_{\text{NO}_2}^2} \frac{P}{P^2} = \frac{X_{\text{N}_2\text{O}_4}}{X_{\text{NO}_2}^2} \frac{1}{P} = K \quad \text{const}$$

If you increase P  
Then the mole fraction of NO<sub>2</sub>  
must go down since K is constant



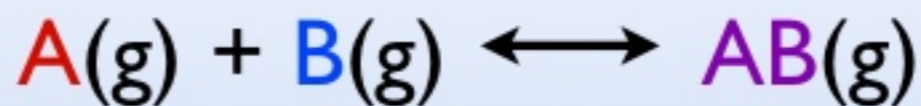
## How to change the pressure (constant T)

Increase P (decrease V) Shifts to side with fewer gas molecules

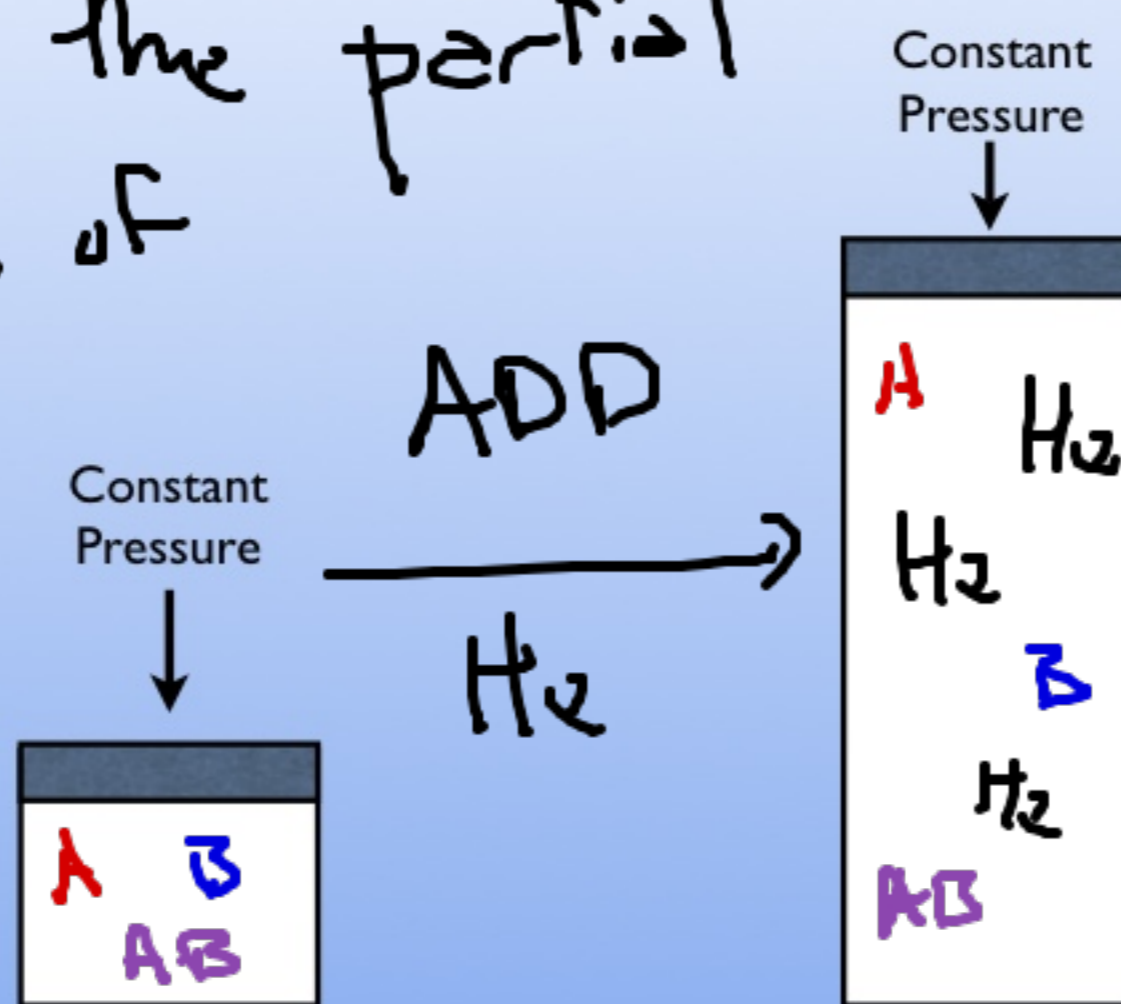
Decrease P (increase V) Shifts to side with more gas molecules

Must be gas.  
Same # of molecules  
└──────────> No effect

# Adding Inert Gas at Constant Pressure



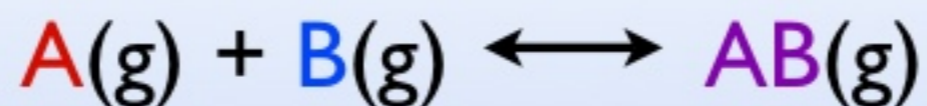
LOWERS the partial pressures of A, B, AB



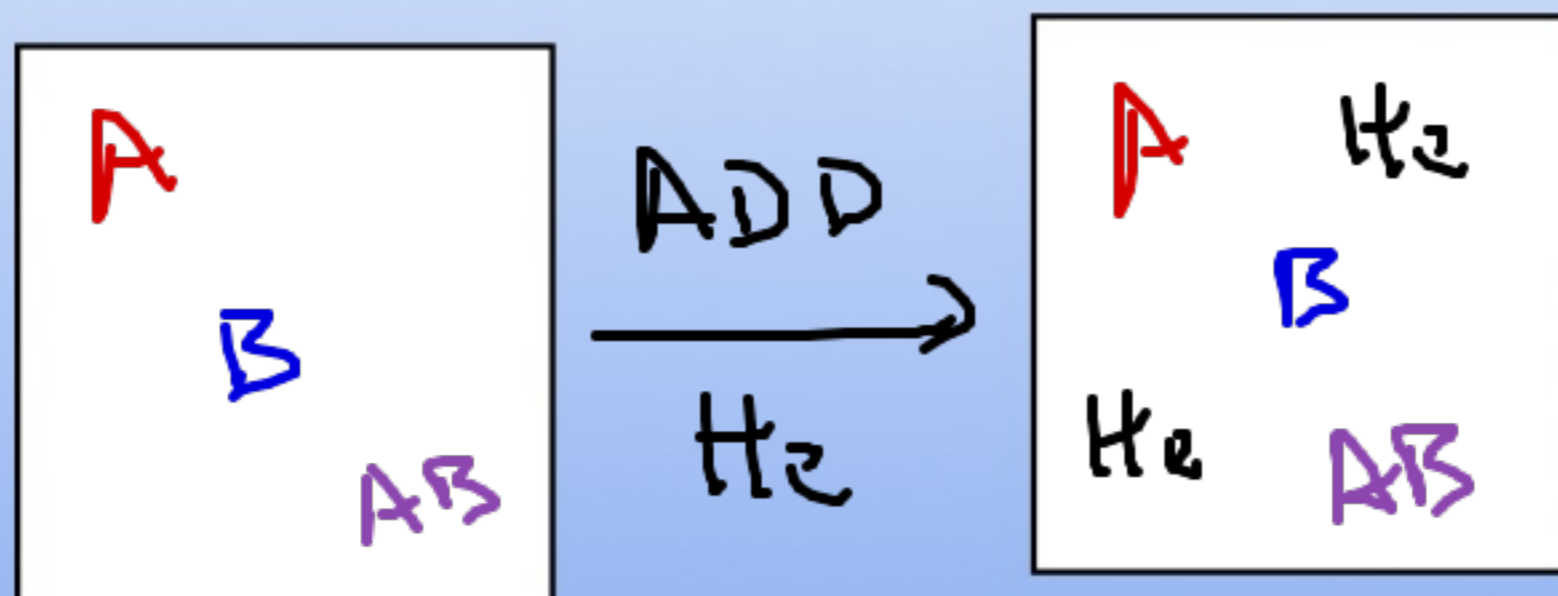
Like lowering the  $P$ !

Effectively Dilutes the Gas

## Adding Inert Gas at Constant Volume



Partial P of A, B, AB unchanged.



NO EFFECT

Effectively Does nothing

## Temperature Change



this reaction is exothermic

$$\Delta H < 0$$

If you increase T then to  
"partially compensate" the reaction  
shifts to the reactants (consuming heat)

T dependence given by  $\Delta H$

Why does Temperature Change Equilibrium?



$$K_c = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3}$$

**K is a function of T!**

$$\Delta_{\text{R}}G^{\circ}(T) = -RT \ln K$$

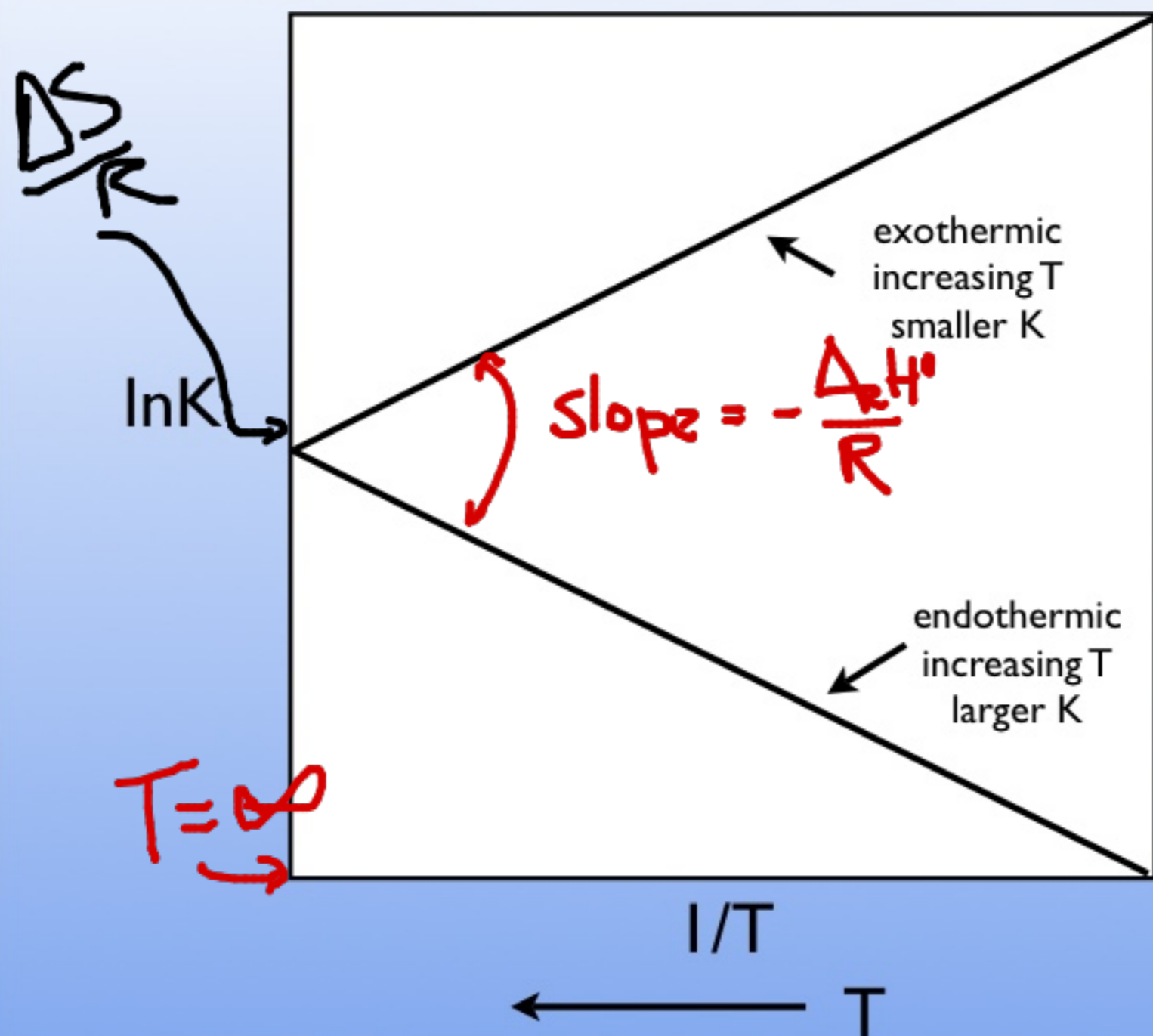
$$\Delta_{\text{R}}G^{\circ}(T) = \Delta_{\text{R}}H^{\circ} - T \Delta_{\text{R}}S^{\circ}$$

$$-RT \ln K = \Delta_{\text{R}}H^{\circ} - T \Delta_{\text{R}}S^{\circ}$$

$$\ln K = -\frac{\Delta_{\text{R}}H^{\circ}}{RT} + \frac{\Delta_{\text{R}}S^{\circ}}{R}$$

Temperature dependence of  $K$  depends on  $\Delta_{\text{R}}H^{\circ}$

$$\ln K = -\Delta_R H^\circ / RT + \Delta_R S^\circ / R$$



$$y = mx + b$$

y is  $\ln K$

x is  $1/T$

m is  $-\Delta_R H^\circ / R$

b is  $\Delta_R S^\circ / R$

a different way to do  
calorimetry  
measure K to find  
 $\Delta_R H^\circ$

Just like Clausius - Clapeyron !!

Can we relate two K's at two Temperatures?

$$\ln K_2 = -\frac{\Delta_r H}{RT_2} + \frac{\Delta_r S}{R}$$

$$- \ln K_1 = -\frac{\Delta_r H^\circ}{RT_1} + \frac{\Delta_r S^\circ}{R}$$

$$\ln \left( \frac{K_2}{K_1} \right) = -\frac{\Delta_r H^\circ}{R} \left[ \frac{1}{T_2} - \frac{1}{T_1} \right]$$